Hybrid ANFIS-ants system based optimisation of turning parameters

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ABSTRACT

Purpose: The paper presents a new hybrid multi-objective optimization technique, based on ant colony optimization algorithm (ACO), to optimize the machining parameters in turning processes.

Design/methodology/approach: Three conflicting objectives, production cost, operation time and cutting quality are simultaneously optimized. An objective function based on maximum profit in operation has been used. The proposed approach uses adaptive neuro-fuzzy inference system (ANFIS) system to represent the manufacturer objective function and an ant colony optimization algorithm (ACO) to obtain the optimal objective value.

Findings: ACO algorithm is completely generalized and problem independent so it can be easily modified to optimize this turning operation under various economic criteria. It can obtain a near-optimal solution in an extremely large solution space within a reasonable computation time.

Research limitations/implications: The developed hybrid system can be also extended to other machining problems such as milling operations. The results of the proposed approach are compared with results of three non-traditional techniques (GA, SA and PSO). Among the four algorithms, ACO outperforms GA and SA algorithms.

Practical implications: An example has been presented to give a clear picture from the application of the system and its efficiency. The results are compared and analysed using methods of other researchers and handbook recommendations. The results indicate that the proposed ant colony paradigm is effective compared to other techniques carried out by other researchers.

Originality/value: New evolutionary ACO is explained in detail. Also a comprehensive user-friendly software package has been developed to obtain the optimal cutting parameters using the proposed algorithm.

Keywords: Machining; Turning optimization, ANFIS-Ants technique

Reference to this paper should be given in the following way:

1. Introduction

The selection of optimal cutting parameters is a very important issue for every machining process in order to enhance the quality of machining products, to reduce the machining costs and to increase the production rate. Do to machining costs of Numerical Control machines (NC), there is an economic need to operate NC machines as efficiently as possible in order to obtain the required pay back. In workshop practice, cutting parameters are selected from machining databases or specialized handbooks, but they don’t consider economic aspects of machining. The cutting conditions set by such practices are too far from optimal. Therefore, a mathematical approach has received much attention as a method for obtaining optimised machining parameters. For the optimisation of a machining process, either the minimum production time or the maximum profit rate is used as the objective function subject to the
Optimization of machining parameters is a difficult work [1], where the following aspects are required: knowledge of machining; empirical equations relating the tool life, forces, power, surface finish, etc., to develop realistic constraints; specification of machine tool capabilities; development of an effective optimization criterion; and knowledge of mathematical and numerical optimization techniques.

### 2. ANFIS-Ants system

The proposed approach consists of two main steps. First, experimental data are prepared to train and test ANFIS system to represent the objective function ($y$). Finally, an ACO algorithm is utilized to obtain the optimal objective value. Figure 1 shows the flowchart of the proposed approach. Figure 2 shows the general ANFIS-ACO based optimization scheme.

**Optimization process:**
1. Entering of input data.
2. Generation of random cutting conditions-initial solutions.
3. Calculation of other values ($P, F, MRR, P; T, Ra, Tp, y$).
4. Preparation of data for training and testing of ANFIS.
5. Use of ANFIS model: The purpose of ANFIS is to predict the manufacturer’s value function ($y$) in case of randomly selected cutting conditions.
6. Training and testing of ANFIS.
7. Optimization process: The cutting conditions where the function ($y$) has the maximum are the optimum cutting conditions. The extreme of the function ($y$). Since the function ($y$) is expressed with ANFIS, it means that the extreme of ANFIS is searched for.
8. Survey of optimum cutting conditions and the variables relevant to them.
9. Graphic representation of results and optimization statistic.

### 3. Turning model formulation

In CNC machine tools, the finished component is obtained through a number of rough passes and finish passes. The roughing operation is carried out to machine the part to a size that is slightly more than its desired size in preparation for the finish cut. The finish cut is called single-pass contour machining, which is machined along the profile contour. In this paper one roughing stage and a finished stage are considered to machine the component from the bar stock.

The objective of this optimization is to determine the optimal machining parameters including cutting speed, feed rate and depth of cut in order to minimize the production cost ($C_p$) and to maximize production rate (represented by manufacturing time ($T_p$)) and cutting quality ($R_q$). The operation of turning is defined as a multi-objective optimization problem with limitation non-equations and with three conflicting objectives (production rate, operation cost, quality of machining). All the above-mentioned objectives are represented as a function of the cutting speed, feed rate and depth of cutting.

<table>
<thead>
<tr>
<th>Step 1</th>
<th>Step 2</th>
</tr>
</thead>
<tbody>
<tr>
<td>Load training/ testing data Generate initial FIS model</td>
<td>Predict responses via ANFIS objective model ($y$)</td>
</tr>
<tr>
<td>ANFIS training and testing</td>
<td>Is stopping criteria reached</td>
</tr>
<tr>
<td>Obtain ANFIS to predict objective (response) function</td>
<td>Print the best function value (optimal solution)</td>
</tr>
<tr>
<td>Create initial solutions</td>
<td></td>
</tr>
<tr>
<td>Predict responses via ANFIS objective model ($y$)</td>
<td></td>
</tr>
<tr>
<td>Set ACO parameters</td>
<td></td>
</tr>
<tr>
<td>ACO search for optimal solution</td>
<td></td>
</tr>
</tbody>
</table>

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**References**

1. [Journal of Achievements in Materials and Manufacturing Engineering](https://doi.org/10.1007/s11814-009-0001-5)

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3.1. Production rate [9]

The production rate is measured as the entire time necessary for the manufacture of a product (T_p). It is the function of the metal removal rate (MRR) and of the tool life (T) [10];

\[
T_p = T_s + V \cdot (1 + \frac{T_c}{T}) / \text{MRR} + T_i
\]  

(1)

where T_s, T_c, T_l, and V are the tool set-up time, the tool change time, the time during which the tool does not cut and the volume of the removed metal. In some operations the T_s, T_c, T_l and V are constants so that T_p is the function of MRR and T. The metal removal rate is expressed as:

\[
\text{MRR} = 1000 \cdot v \cdot f \cdot a
\]  

(2)

3.2. The cost function [9]

The unit production cost, C_p, for turning operations can be divided into three basic cost elements: the tool cost and tool
replacement cost \( (C_r) \), cutting cost by actual time in cut \( (C_c) \) and overhead cost \( C_0 \). \( T \) is tool life. Formula for calculating the above cost is used as given by [9]. Finally, by using the mathematical manipulations, the unit production cost can be obtained as:

\[
C_p = T_p \cdot (C_1/T + C_1 + C_0)
\]

(3)

3.3. Cutting quality [9]

The most important criterion for the assessment of the surface quality is roughness calculated according to [9]:

\[
R_a = k \cdot v^{x_1} \cdot f^{x_2} \cdot a^{x_3}
\]

(4)

where \( x_1, x_2, x_3 \) and \( k \) are the constants relevant to a specific tool-workpiece combination.

3.4. Cutting condition constraints

The practical constraints imposed during the roughing and finishing operations are stated as follows [9].

Parameter bounds. The available range of cutting speed, feed rate and depth of cut are expressed in terms of lower and upper bounds. The bounds on feed rate and depth of cut is setup for the safety of the operator. The parameter bound values and constants are:

- \( v_{\text{min}} \leq v \leq v_{\text{max}} \)
- \( f_{\text{min}} \leq f \leq f_{\text{max}} \)
- \( a_{\text{min}} \leq a \leq a_{\text{max}} \).

Tool-life constraint. The constraint on the tool life is taken as

\[ T_{\text{min}} \leq T \leq T_{\text{max}}. \]

Power constraint. The power required during the cutting operation should not exceed the available power of the machine tool. The power is given as:

\[
P = \frac{k_f \cdot f^{1.1} \cdot d^{0.7} \cdot v}{6120 \eta}
\]

(5)

where \( k_f, \mu \) and \( \eta \) are the constants pertaining to specific tool-work piece combination and \( \eta \) is the power efficiency. The limitations of the power and cutting force are equal to: \( P(v, f, a) \leq P_{\text{max}} \).

In order to ensure the evaluation of mutual influences and the effects between the objectives and to be able to obtain an overall survey of the manufacturer’s value system the multi-attribute function of the manufacturer \( (y) \) is determined. The cutting parameter optimization problem is formulated as the following multi-objective optimization problem: \( \text{min } T_p (v, f, a), \text{min } C_p (v, f, a), \text{min } R_a (v, f, a) \).

\[
y = 0.42 \cdot e^{(-0.225T_p)} + 0.1 \cdot t^{(0.256T_a)} + \frac{0.05}{(f + 1.25 \cdot C_p \cdot R_a)}
\]

(6)

Using a given input/output data set, the ANFIS method constructs a fuzzy inference system (FIS) whose membership function parameters are tuned using either a backpropagation algorithm alone, or in combination with a least squares type of method. This allows fuzzy systems to learn from the data they are modeling. FIS Structure is a network-type structure similar to that of a neural network, which maps inputs through input membership functions and associated parameters, and then through output membership functions and associated parameters to outputs.

ANFIS applies two techniques in updating parameters. For premise parameters that define membership functions, ANFIS employs gradient descent to fine-tune them.

4. Objective function modelling

First step uses an adaptive neuro fuzzy inference system (ANFIS) to model the response (manufacturer’s implicit multiattribute) function \((y)\). The variables of this problem are velocity, feedrate \((f)\) and depth of cutting \((a)\). The output from the system is a real value \((y)\). The relationship between the cutting parameters and manufacturer objective function is first captured via a neural network and is subsequently reflected in linguistic form with the help of a fuzzy logic based algorithm. Algorithm uses training examples as input and constructs the fuzzy if-then rules and the membership functions of the fuzzy sets involved in these rules as output.

Figure 3 shows the fuzzy rule architecture of ANFIS when triangular membership function is adopted. The architectures shown in Figure 3 consist of 32 fuzzy rules. During training in ANFIS, 140 sets of experimental data were used to conduct 400 cycles of training.

ANFIS has proved to be an excellent universal approximator of non-linear functions. If it is capable to represent the manufacturer’s implicit multiattribute function.
For consequent parameters that define the coefficients of each output equations, ANFIS uses the least-squares method to identify them. This approach is thus called Hybrid Learning method since it combines the gradient descent method and the least-squares method.

ANFIS modeling process starts by:
1. Obtaining a data set (input-output data pairs) and dividing it into training and checking data sets.
2. Finding the initial premise parameters for the membership functions by equally spacing each of the membership functions.
3. Determining a threshold value for the error between the actual and desired output.
4. Finding the consequent parameters by using the least-squares method.
5. Calculating an error for each data pair. If this error is larger than the threshold value, update the premise parameters using the gradient descent method as the following: \( Q_{\text{next}} = Q_{\text{nov}} + \eta \), where \( Q \) is a parameter that minimizes the error, \( \eta \) the learning rate, and \( d \) is a direction vector.
6. The process is terminated when the error becomes less than the threshold value. Then the checking data set is used to compare the model with actual system. A lower threshold value is used if the model does not represent the system.

After training the estimator, its performance was tested under various cutting conditions.

Test data sets collected from a wide range of cutting conditions in turning were applied to the estimator for evaluating objective function \( y \). The performance of this method turned out to be satisfactory for estimating of objective function \( y \), within a 2% mean percentage error.

Once a multi-attribute value function is assessed and validated the ANFIS is used to decipher the manufacturer’s overall preference and the multi-objective optimization problem will be reduced to a single objective maximization problem as follows:

\[
\max_{v,f,a} y[p(v, f, a), C_p(v, f, a), R_a(v, f, a)]
\]  \( (7) \)

5. ACO algorithm

Ant colony optimization is a non-traditional optimization technique in which the main idea underlying it is that of a parallelizing search over several constructive computational threads, all based on a dynamic memory structure incorporating information on the effectiveness of previously obtained results and in which the behavior of each single agent is inspired by the behavior of real ants.

Special insects like ants, termites, and bees that live in a colony are capable of solving their daily complex life problems. These behaviors which are seen in a special group of insects are called swarm intelligence. Swarm intelligence techniques focus on the group’s behavior and study the decentralized reactions of group agents with each other and with the environment. The swarm intelligence system includes a mixture of simple local behaviors for creating a complicated general behavior and there is no central control in it. Ants have the ability to deposit pheromone on the ground and to follow, in probability, pheromone previously deposited by other ants. By depositing this chemical substance, the ants leave a trace on their paths. By detecting this trace, the other ants of the colony can follow the path discovered by other ants to find food. For finding the shortest way to get food, these ants can always follow the pheromone trails. This cooperative search behavior of real ants inspired the new computational paradigm for optimizing real life systems and it is suited for solving large scale optimization problem.

The first ACO algorithm, called ant system (AS) has been applied to the travelling salesman problem (TSP). Dorigo [7], proposed an ant colony optimization methodology for machining parameters optimization in a multi-pass turning model, which originally was developed by [8].

Recently, a modified ACO was presented as an effective global optimization procedure by introducing bi-level search procedure called local and global search. The important aspect in ACO is that the artificial ants select the solution.

5.1. Process optimization using ACO

The proposed continuous ant colony algorithm for optimization of cutting conditions in multi-pass turning is shown as scheme in Figure 4. The distribution of ants is shown in Figure 5.

**Initial solution.** An initial solution of N will consist of 160 randomly generated solutions, with values that lie in the range of allowable cutting speed, depth of cut and feedrate. The 160 solutions are then sorted in ascending order with respect to the objective function.

The regions pertaining to minimum production cost are referred to as superior solutions, while regions pertaining to the maximum production cost are referred to as inferior solutions.

**Distribution of ants.** The total numbers of ants, \( A \), is 80, which is half of N and is distributed as 72 for global (G) and 8 for local search (L).

An ACO utilizes bi-level procedures which include local and global searches.

**Local search:** With a local search, the L local ants select L regions from N regions and move in search of better fitness. Here L is 6, and L solutions are selected as per the current pheromone trail value. Local search ants select a region L with a probability \( P_i(t) = \tau_i(t) / \sum \tau_i(t) \), where \( i \) is the region index and \( \tau_i(k) \) is the pheromone trail on region \( i \) at time \( t \). After selecting the destination the ant moves through a short distance (finite random increment 0.005).

**Updating the pheromone trail value of new solution in local search.** If the fitness is improved, the new solutions are updated to the current region. Correspondingly the regions position vector is updated. The variables of this problem are cutting speed, feedrate, depth of cut, all of which can have any continuous value subject to the limits imposed. The objective functions are calculated for each solution.

In the continuous algorithm, the pheromone values are decreased after each iteration by:

\[
\tau_i(t + 1) = \rho \cdot \tau_i(t)
\]  \( (8) \)
After selecting the destination, the ant solutions. The following three operations are performed on the regions by replacing the inferior solutions of the existing

where \( \rho \) is the evaporation rate which is assumed to be 0.2 on a trial basis and \( t_\ast(t) \) is the trail associated with solution at time \( t \).

Fig. 4. Scheme of the ACO algorithm

Global search. Using global search, global ants create \( G \) new regions by replacing the inferior solutions of the existing solutions. The following three operations are performed on the randomly generated initial solution: (a) Random walk or cross over \(-90\%\) of the solutions (randomly chosen) in the inferior solutions are replaced with randomly selected superior solutions; (b) Mutation – the process where by randomly adding or subtracting a value is done to each variable of the newly created solutions in the inferior region with a mutation probability; and (c) Trial diffusion – applied to inferior solutions that were not considered during random walk and mutation stages.

A global search is done sequentially by crossover, mutation and trial diffusion operations. The subsequent values of the variables of the child are set to the corresponding value of a randomly chosen parent with a crossover probability (0.75). Mutation operation adds or subtracts a value to/from each variable with mutation probability. The mutation step size is the same as the above distance \( \Delta(T, R) \). After selecting the destination, the ant moves through a short distance \( \Delta(T, R) = R(1 - t^{0.75}) \), where \( R \) is maximum search radius, \( r \) is a random number from \([0,1]\), \( T \) is the total number of iterations of the algorithm.

Performing an ACO, ants are repeatedly sent to trail solutions in order to optimize the objective value. The total number of ants (denoted by \( A \)) is set as half the total number of trail solutions (denoted by \( S \)).

Trail diffusion. Here, two parents are selected at random from the parents region. The child can have:

1) the value of the corresponding variable of the first parent;
2) the value of the corresponding variable of the second parent;

or

3) a combination arrived from the weighted average of the above

\[ x_{\text{child}} = \alpha \cdot x_{\text{parent 1}} + (1 - \alpha) \cdot x_{\text{parent 2}} \]

where \( \alpha \) is a uniform random number in the range \([0,1]\). The probability of selecting the 3rd option is set equal to the mutation probability 0.75, and the probability of selecting the 1st and 2nd options is allotted a probability of 0.2.

Updating of pheromone trail value of new solution in global search.

After the global search, the pheromone trail value of the new solutions is updated proportionally to the improvement in the objective value.

Sort the regions according to the function value. New solutions will be obtained after the global and local search. The solutions will also have the new pheromone trail values.

The solutions are sorted in ascending order of the objective values and the best objective value is stored. The process is repeated for a specified number of iterations.

Fig. 5. Distribution of search points (ants) in ACO algorithm
The ACO algorithm:
Step 1. Set parameter values including: S, A, \( \alpha \), \( \beta \), \( \gamma \), \( P_c \), \( P_m \), T, R, and bounds of each control factor.
Step 2. Create S trail solutions (v, f, a). Estimate the objective value of the trail solutions through the ANFIS model (y).
Step 3. Set the initial pheromone value of all trails.
Step 4. Repeat steps 6-8 until the stopping criteria has reached.
Step 5. Send L ants to the selected trail solutions for local search.
Step 6. If the solution is improved, move the ants to the new solution and update the pheromone value.
Step 7. Send G ants to global trails and generate their offspring by crossover and mutation.
Step 8. Evaporate pheromone for all trails.

From the graphs (Figure 6 and 7) the maximum profit rate results are observed.

Table 1.
Comparison of results for ANFIS-ACO, GA, LP and PSO approach

<table>
<thead>
<tr>
<th>No.</th>
<th>Algorithm</th>
<th>Constraint set</th>
<th>Runs</th>
<th>Optimum solution</th>
<th>Average optim. time [s]</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td>( v_{opt} ) [m/min]</td>
<td>( f_{opt} ) [mm/rev]</td>
</tr>
<tr>
<td>1</td>
<td>PSO [12,13]</td>
<td>tool-life; cutting force-power; surface roughness;</td>
<td>1 - 25</td>
<td>101.211</td>
<td>0.231</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>1 - 150</td>
<td>103.377</td>
<td>0.217</td>
</tr>
<tr>
<td>2</td>
<td>Proposed ANFIS-ACO</td>
<td>tool-life; cutting force-power; surface roughness;</td>
<td>1 - 25</td>
<td>95.1926</td>
<td>0.3793</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>1 - 150</td>
<td>97.433</td>
<td>0.2934</td>
</tr>
<tr>
<td>3</td>
<td>SA [14]</td>
<td>tool-life; cutting force-power; surface roughness;</td>
<td>1 - 1000</td>
<td>112.852</td>
<td>0.194</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>1 - 1400</td>
<td>108.464</td>
<td>0.221</td>
</tr>
<tr>
<td>4</td>
<td>GA [15]</td>
<td>tool-life; cutting force-power; surface roughness;</td>
<td>1 - 150</td>
<td>102.165</td>
<td>0.039</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>1 - 500</td>
<td>98.122</td>
<td>0.313</td>
</tr>
</tbody>
</table>

Fig. 6. ACO optimization graph

Fig. 7. GA optimization graph
6. Analysis of results and discussion

The ant colony optimization method combined with ANFIS prediction system was tested on the CNC lathe GF02. The work piece material is mild steel (CK45) and the tool material has a carbide tip. The task is to find optimum cutting conditions for the process of turning with minimal costs. Proposed ACO approach was compared with three non-traditional techniques (GA, SA and PSO). The results obtained from four techniques are given below in Table 1. All the parameters and constraint sets are the same in all four cases. There is a total of 4 constraints. Cutting forces and their influence on the economics of machining is summarized according to investigation of Kopac [11]. The proposed model is run on a PC 586 compatible computer using the Matlab language. The results revealed that the proposed method significantly outperforms the GA and SA approach. The proposed approach found an optimal solution of 12.461 for as low as 1-18 runs the genetic-based approach require as much as 1-500 runs to find an solution of 14.661. This means that the proposed approach has 16.02% improvement over the solution found by GA approach and 23.08% over SA approach. Moreover, the simulated annealing approach (SA/PSO) of [14] also generated an inferior solution of 17.24 for as much as 901–1000 runs which means that the optimal solution of ACO algorithm has an improvement of 23.6%. It is observed that PSO has outperformed all other algorithms [15]. Next ACO, SA and GA are ranked according to costs obtained from algorithms. The costs obtained and optimum machining conditions are shown in Table 1. From the results, it is clear that the proposed ACO approach significantly outperforms the other two methods, such as GA and SA. Clearly, the ACO approach provides a sufficiently approximation to the true optimal solution.

7. Conclusions

In this work, non-conventional optimization techniques ACO has been studied for the optimization of machining parameters in turning operations.

The hybrid ANFIS-ants integrates neural network, fuzzy logic and continuous ant colony optimization to model the machining system and to optimize machining process. ACO algorithm is completely generalized and problem independent so that can be easily modified to optimize this turning operation under various economic criteria. It can obtain a near-optimal solution in an extremely large solution space within a reasonable computation time.

The algorithm can also be extended to other machining problems such as milling operations. The results of the proposed approach are compared with results of three non-traditional techniques (GA, SA and PSO). Among the four algorithms, PSO outperforms all other algorithms.

References